

SEARCH ENGINE COMPETITION WITH NETWORK EXTERNALITIES

Cédric Argenton* & Jens Prüfer†

ABSTRACT

The market for Internet search is not only economically and socially important, it is also highly concentrated. Is this a problem? We study the question of whether “competition is only a free click away.” We argue that the market for Internet search is characterized by indirect network externalities and construct a simple model of search engine competition, which produces a market share development that fits well the empirically observed developments since 2003. We find that there is a strong tendency toward market tipping and, subsequently, monopolization, with negative consequences on economic welfare. Therefore, we propose to require search engines to share their data on previous searches. We compare the resulting “competitive oligopoly” market structure with the less-competitive current situation and show that our proposal would spur innovation, search quality, consumer surplus, and total welfare. We also discuss the practical feasibility of our policy proposal and sketch the legal issues involved.

JEL: L10; K23; L86

I. INTRODUCTION

*There’s always a concern that large private collections of data are not available to search engines We’ve taken a position, both in a religious and in a business perspective, that the world is better off if you take the information that you’re assembling and make it accessible.*¹

Eric Schmidt, then CEO of Google

* Assistant Professor, Department of Economics, Tilburg University; CentER, Tilburg University; Research Coordinator, Tilburg Law and Economics Center (TILEC), Tilburg University. Email: c.argenton@uvt.nl.

† Assistant Professor, Department of Economics, Tilburg University; Senior Member, TILEC, Tilburg University; Research Fellow, CentER for Economic Research, Tilburg University. We are grateful to Erik Brynjolfsson, Lapo Filistrucchi, Joshua Gans, Damien Geradin, Michael Grubb, Pierre Larouche, Catherine Tucker, anonymous referees, and seminar or conference participants at Tilburg University and Northwestern University for comments on a previous draft of this article. All errors are our own. We wish to disclose that TILEC has entered into a sponsorship agreement with Microsoft Inc., although neither this research nor any other of our respective research projects is currently funded under this program.

¹ See E.B. Boyd, *Google on Facebook-Bing Social Search: What, Us Worry?*, FAST COMPANY, Oct. 14, 2010, <http://www.fastcompany.com/1695187/google-on-social-search-who-us-worried>.

The market for Internet search has grown from virtually zero in the mid-1990s to a multibillion dollar business nowadays. Internet search revenues in the United States totaled \$5.7 billion for the first six months of 2010, an increase by 11.6 percent from the same period in 2009.² On top of this direct economic significance, search engines are crucially important both for Internet users looking for information and for businesses who want to sell goods and services to those users. Although information is abundant on the World Wide Web, users' attention is limited. Search engines serve as gatekeepers between the information and services provided online and searchers' attention.

The market for Internet search is not only economically and socially important, it is also highly concentrated. In the United States, Google had a market share of 66.2 percent, Yahoo! of 16.4 percent, and Bing of 11.80 percent, as of November 2010.³ In the United Kingdom, just as in many other European countries, Google had a market share of 90.83 percent, Yahoo! of 3.21 percent, and Bing of 3.12 percent, as of December 2010.⁴ Note that Bing is Microsoft's search engine and that, in early 2010, Yahoo! in effect sold its search and search advertising business to Microsoft.⁵

Is high market concentration a problem? For many, the main concern is Google's seemingly dominant position and the market power that comes with it.⁶ Indeed, several competition authorities have opened (and in some cases, closed) investigations into the market behavior of Google. Most notably, on November, 30 2010, the European Commission launched a formal inquiry into allegations that Google has been manipulating the results of searches in ways that unfairly benefit it.⁷ Other matters up for investigation include the ad pricing scheme applied to rival providers of online services, as well as exclusivity obligations imposed on advertisers.⁸ (Related complaints have been brought before the French, Italian, and German competition authorities.⁹) On April, 8 2011, the U.S. Department of Justice (DOJ) and Google proposed a settlement in the case of the intended

² PwC, IAB Internet Advertising Revenue Report, at 13 (2010), available at http://www.iab.net/media/file/IAB_report_1H_2010_Final.pdf.

³ Press Release, comScore, comScore Releases November 2010 U.S. Search Engine Rankings (Dec. 15, 2010).

⁴ See Kris, What Is Search Marketing?, Type Media (posted Jan. 16, 2011), <http://www.type-media.co.uk/search-marketing/what-is-search-marketing>.

⁵ See Jared Newman, *Will Bin's Back-End Make Yahoo Better?*, PCWORLD, Aug. 25, 2010, http://www.pcworld.com/article/204134/will_bings_backend_make_yahoo_better.html.

⁶ There are other reasons for concern about the market for search engines, which we do not take as the primary objects of this study: media pluralism and privacy rights come to the forefront.

⁷ Press Release, Eur. Comm'n, Antitrust: Commission Probes Allegations of Antitrust Violations by Google (Nov. 30, 2010), <http://europa.eu/rapid/pressReleasesAction.do?reference=IP/10/1624>.

⁸ *Id.*

⁹ See, e.g., Italian Newspapers Ask Competition Watchdog to Investigate Google News, OUTLAW.COM, Aug. 31, 2009, <http://www.out-law.com/page-10336>.

acquisition of ITA Software, Inc. by Google.¹⁰ The DOJ required Google to further develop, firewall, and license ITA's shopping software under a rather intrusive firewalling and monitoring regime.¹¹ On June, 24 2011, the *Wall Street Journal* indicated that the U.S. Federal Trade Commission was to open a formal investigation of Google's business practices, a move since confirmed by Google in regulatory filings.¹²

On the other hand, given the characteristics of the search engine market, in particular the very modest switching cost for users, it is not obvious that high market concentration is detrimental to innovation and economic welfare and that government intervention should be considered. On July, 16 2010, following an extended series of articles on Google's market position, *The Financial Times* concluded: "it is better for different search engines to compete vigorously with each other to produce the best and most relevant results. Google may be highly successful in search but competition is only a free click away."¹³ This viewpoint draws on the economic theory of contestable markets, which holds that an incumbent with market power cannot exploit consumers as long as it must fear that competitors would just step in and offer their services at lower prices.¹⁴

The appropriateness of this viewpoint is exactly the starting point of our research. In this article, we do *not* try to answer the question of whether Google has abused a dominant position. By contrast, we study the question whether it is true that "competition is only a free click away." In a crucial sense, this question is anterior to any discussion of monopolization, dominance, or abuse. If the market for search engines is highly contestable, then those discussions are moot: Google's high market share can then be taken as an indication that it is simply the best search engine technology currently available.¹⁵ Conversely, if the market is poorly contestable or non contestable, then its structure, rather than the conduct of any of the participants, is likely to be problematic and to call for direct regulatory intervention rather than antitrust action.

¹⁰ Press Release, U.S. Dep't of Justice, Justice Department Requires Google Inc. to Develop and License Travel Software in Order to Proceed with Its Acquisition of ITA Software Inc. (Apr. 8, 2011), <http://www.justice.gov/opa/pr/2011/April/11-at-445.html>.

¹¹ *Id.*

¹² Thomas Catan & Amir Efrati, *Feds to Launch Probe of Google*, WALL ST. J., June 24, 2011, <http://online.wsj.com/article/SB10001424052702303339904576403603764717680.html>.

¹³ *Google Should Be Watched Carefully*, FINANCIAL TIMES, July 15, 2010, <http://www.ft.com/cms/s/0/a84e8438-9049-11df-ad26-00144feab49a.html#axzz1izSgsNzm>.

¹⁴ For a classical exposition, see WILLIAM J. BAUMOL, JOHN C. PANZAR & ROBERT D. WILLIG, *CONTESTABLE MARKETS AND THE THEORY OF INDUSTRY STRUCTURE* (Harcourt Brace Jovanovich 1982).

¹⁵ Whether the behavior of a market participant is susceptible to give rise to antitrust liability remains, of course, of prime *legal* interest even in that case, but there is no reason to expect the enforcement of competition law to lead to a significantly different market outcome in the medium run.

Thus, in this article, we do not study, or take a stance on, the allegedly abusive behavior of search engines in general or of Google in particular. Rather, we try to understand what determines the quality of a search engine as perceived by users. On this basis, we provide a simple model of quality-based search engine competition. Interestingly, our model can be interpreted in terms of research and development (R&D) investment and innovation. We argue that the current market structure is not stable and that the search engine market displays a strong structural tendency toward monopolization. This has negative effects on the expected average search quality, the rate of innovation, consumer surplus, and total welfare.

Our key insight is that the production of search quality is characterized by a peculiar (intertemporal) type of *indirect network externalities*. We argue that such indirect externalities arise in the market for search engines because users will not consider, when deciding whether to run another query, that the results of their query and subsequent clicking behavior on suggested links are stored by the search engine. Currently, this information, also known as *query logs* or *search logs*, is not public. Only the search engine that is used to run the query can aggregate it with the information gained from other users who entered a similar search keyword. It can thereby improve its guess as to what future users—on average or with certain revealed characteristics such as geographical location or language—are looking for when they enter a certain keyword. This translates into higher search quality perceived by users.

The importance of large amounts of query log data for producing search engine quality has been widely acknowledged by the computer science literature.¹⁶ Access to more search log data today leads to higher perceived search quality. Higher perceived search quality leads to more demand for searches tomorrow, which in turn creates even more search log data tomorrow than today. This mechanism is at the core of the model by which we propose to analyze competition in the search engine market.

Taking everything else equal, this implies for a competitive market that a firm that had a modest lead in market share at some point in time can increase that advantage more and more, whereas the other firms' market shares decrease more and more. That is, the market "tips."

¹⁶ Amanda Spink, Dietmar Wolfram, Major B. J. Jansen & Tefko Saracevic, *Searching the Web: The Public and Their Queries*, 52 J. AM. SOC'Y FOR INFO. SCI. & TECH. 226 (2001); Bernard J. Jansen, Mimi Zhang & Ying Zhang, Brand Awareness and the Evaluation of Search Results, World Wide Web Conference Poster Paper (2007); Carrie Grimes, Diane Tang & Daniel M. Russell, Query Logs Alone Are Not Enough, World Wide Web Conference Paper (2007), available at http://dmrussell.googlepages.com/query_logs_are_not_enough_2007_02_12.pdf; Ziv Bar-Yossef & Maxim Gurevich, Mining Search Engine Query Logs via Suggestion Sampling, Very Large Data Bases Conference Paper (2008); Steven Levy, *Secret of Googlenomics: Data-fueled Recipe Brews Profitability*, WIRED MAG., June 17, 2009, available at http://www.wired.com/culture/culturereviews/magazine/17-06/nep_googlenomics; F. Silvestri, *Mining Query Logs: Turning Search Usage Data into Knowledge*, 4 FOUND. & TRENDS IN INFO. RETRIEVAL 1 (2010).

To remedy this situation, we put forward and analyze the following policy proposal: *All search engines should be required to share their (anonymized) data on clicking behavior of users following previous search queries.*

We study the resulting market structure, coined a “competitive oligopoly,” and show that it dominates alternative market structures in all the above-mentioned dimensions. If we compare it with today’s market structure, the disadvantage of the competitive oligopoly is that the costs of producing quality “investments” are multiplied. However, we can show that the competing firms would have no incentive to decrease their quality below the quality of today’s dominant firm (Google). In addition, *all* users would benefit from high quality, and *all* search engines’ incentives to innovate would remain consistently high.

Although the implications of the externality we uncover have not been stressed in the academic literature thus far, the point itself is perceived by practitioners. For instance, when the DOJ cleared the alliance between Yahoo! and Microsoft in February 2010, it stated that Microsoft’s access to Yahoo!’s search query data would speed up Bing’s automated learning, helping the search engine return more relevant results, in particular with respect to rare queries.¹⁷ However, to our knowledge the ultimate conclusions from this line of reasoning have not been drawn.

Part II of this article discusses search engine quality, learning effects, and network externalities in more detail and relates our article to the existing literature. In Part III, we introduce a simple model of search engine competition and solve for the equilibria of a row of market structures that are likely to follow one another without governmental intervention. In Part IV, we state our main policy proposal and show that (and why) a competitive oligopoly dominates market structures without intervention. We also discuss the technical feasibility, legal basis, and practical implementation of our proposal. In Part V, we conclude by outlining the tradeoffs involved in any public intervention in this high-tech sector. Technical details and computations are relegated to the Appendix.

II. SEARCH ENGINE QUALITY, NETWORK EXTERNALITIES, AND RELATED LITERATURE

A. Search Engine Quality and Network Externalities

To develop an appropriate model of search engine competition, we first try to understand the question: what actually is search engine quality? In a

¹⁷ See Press Release, U.S. Dep’t of Justice, Statement of the Department of Justice Antitrust Division on Its Decision to Close Its Investigation of the Internet Search and Paid Search Advertising Agreement Between Microsoft Corporation and Yahoo! Inc. (Feb. 18, 2010) [hereinafter U.S. DOJ Statement on Microsoft Yahoo! 2010].

recent survey asking more than 1,100 software testers from more than 50 countries for the “most important attribute in choosing a search engine,” 71 percent chose “overall accuracy of search results.”¹⁸ Other important attributes mentioned were “page load speed” and “real-time relevance.” In the ranking made up in that survey, Google came first in all three categories, followed by Bing and Yahoo!

Based on these survey results, search engine quality may be proxied by the expected time a user needs to obtain a satisfactory result to his search query. What determines this expected time? It depends on the inputs into the search, namely, (1) the sophistication of the search algorithm (algorithm quality), (2) the computer power of the server farms searched by the algorithm (hardware quality), and (3) the amount of potentially relevant data that the algorithm can search through (data quality). Data quality has several parts, among them (3.a) the amount of raw data available online (virtually all data stored on the Internet, at least on the World Wide Web) and (3.b) the context-specific data created by previous searches of a keyword and subsequent clicks by other users.¹⁹ Notably, whereas everybody who has sufficient hardware quality can virtually copy the Internet, which makes (3.a) *public* information, the context-specific data created by previous searches are kept secret by the search engines and, thus, constitute valuable *private* information.²⁰

Hardware quality (2) and the amount of raw data available online (3.a) can be taken to be equal across competitors with sufficiently deep pockets. Consequently, differences in users’ perceived quality of search engines, as

¹⁸ See uTest, Q3 2009 Bug Battle Report: Battle of the Search Engines (2009), available at http://www.utest.com/sites/default/files/uTest%20Q3_09%20Search%20Engine%20Bug%20Battle.pdf.

¹⁹ Search engines also seek to gather other types of data, such as information about a user’s profile and preferences by monitoring click-through rates to contents or online purchasing behavior, a point stressed by Daneil F. Spulber, *The Map of Commerce: Internet Search, Competition, and the Circular Flow of Information*, 5 J. COMPETITION L. & ECON. 633 (2009). To some extent, Google’s business model has recently consisted of providing users with free ancillary applications (including e-mail, calendar, personal page management system, browser, and others) that generate traffic in the first place and can be used to collect such individual-level information. We do not think, however, that this information is subject to network externalities of the type that we stress in this article, as it is specific to a particular user.

²⁰ See Levy, *supra* note 16, for a lively account of the importance of such data. Amanda Spink, Dietmar Wolfram, Major B. J. Jansen & Tefko Saracevic, *Searching the Web: The Public and Their Queries*, 52 J. AM. SOC’Y FOR INFO. SCI. & TECH. 226 (2001) noted that query logs “provide a snapshot for comparison of public behavior while searching, a behavior that can also serve as a clue for improvement of search engines.” *Id.* at 233. It is technically possible to sample search engines’ drop-down suggestion menus as a way to indirectly mine their query logs of a particular engine, but this is no substitute for directly processing those logs. See, e.g., Ziv Bar-Yossef & Maxim Gurevich, *Mining Search Engine Query Logs via Suggestion Sampling* (presented at the Very Large Data Base (VLDB) Conference, 2008).

reported above, must be rooted in differences in algorithm quality (1) and access to context-dependent data (3.b).

Let us take the sophistication of the search algorithm (1) fixed and consider a market where there is some private data (3.b) to be searched. Note that algorithm quality (1) is potentially unequal across search engines (and probably is in practice). In this article, however, we want to isolate the effect that the existence of some private data (3.b) has on the market equilibrium and abstract from the additional effects of heterogeneous algorithms. Moreover, it is an open issue as to how important access to query log data (3.b) is for the production of search quality relative to the other input factors (1) through (3.a). However, we believe we are making an important step toward answering this question by showing that a model that focuses entirely on differences in access to query log data—and holding all other dimensions of competition equal—can generate several empirically observed developments in the search engine industry.²¹ We will return to these points in the conclusion of this article.

We posit that the context-specific data created by searches of a keyword and subsequent clicks by users are not only private but are also characterized by indirect network externalities. If a search engine user decides whether to make another query, she trades off the expected private benefits (getting accurate search results) and the expected private costs (time or opportunity costs) of that query. However, the user will not take into account that her query and her subsequent clicking behavior for this or for that search result provides the search engine with information about user preferences in general. This information allows the search engine to produce search results to the same keywords that are more likely to meet future users' preferences and, thereby, to increase its *perceived* search quality.

Based on this insight, we study the following questions: What are the effects of network externalities on competition among search engines? What are the effects of competition among search engines on economic performance (rate of innovation, consumer surplus, and welfare)? Do these results warrant intervention of public authorities? If so, what type of intervention would be both appropriate and feasible?

B. Related Literature

On a theoretical level, there is now a voluminous literature on network externalities.²² This literature stresses early-mover advantages in the launch of network goods, natural market dominance (competition *for* the market and

²¹ See Part III. For a comparison of several key predictions of the model with reality.

²² Good points of entry include Stanley M. Besen & Joseph Farrell, *Choosing How to Compete: Strategies and Tactics in Standardization*, 8 J. ECON. PERSP. 673 (1994); Nicholas Economides, *The Economics of Networks*, 14 INT'L J. INDUS. ORG. 117 (1996); CARL SHAPIRO & HAL R. VARIAN, *INFORMATION RULES: A STRATEGIC GUIDE TO THE NETWORK ECONOMY* (Harvard Bus. Rev. Press 1999).

“market tipping”), and the strategic importance of compatibility decisions. Markets with network goods are affected by various instances of market failures: consumers might coordinate on the wrong platform or fail to switch to a more efficient one when it becomes available; conversely, firms might fail to coordinate on a unique standard, which prevents consumers from fully taking advantage of network externalities. In addition, dominant firms may fail to provide the right network scope. Public authorities may try to correct or alleviate those market failures, but they face an especially difficult task, given the specific nature of network industries.²³ In this article, we will indeed stress the complexity of the sector but argue that a specific, limited public intervention is possible to restore a level playing field and increase economic welfare.

Direct network externalities usually arise on the demand side, as in the usual example of a communications network. Consumers derive more utility from the network the higher the number of other consumers who choose to connect. Interestingly, the indirect intertemporal externalities we describe can also be viewed as a special version of the *learning curve hypothesis*, a supply-side phenomenon. Economists speak of a learning curve when the current cost of production negatively depends on the cumulative amount produced in the past. This idea dates back at least to Kenneth Arrow’s seminal 1962 article on learning by doing.²⁴ and the Boston Consulting Group helped popularize the concept in the 1970s by stressing the importance of being a first mover and investing in market share.²⁵ It is a well-known phenomenon, early observed, for instance, in the production of aircrafts.²⁶ For search engines, previous queries are instrumental in decreasing the cost of producing quality today. An interesting twist is that, here, contrary to the case of aircraft manufacturing, it is not the *intangible* process of production of earlier units in a particular plant that gives rise to learning, but *recorded* information about past searches. Thus, we have a new type of learning effects whose very nature

²³ For detailed analyses of the policy implications of this line of research, see Nicholas Economides, *Antitrust Issues in Network Industries*, in *THE REFORM OF EC COMPETITION LAW: NEW CHALLENGES* 343 (Ioannis Lianos & Ioannis Kokkoris eds., Kluwer Int’l Law 2010); Neil Gandal, *Compatibility, Standardization and Network Effects: Some Policy Implications*, 18 *OXFORD REV ECON. POL’Y* 80 (2002).

²⁴ Kenneth J. Arrow, *The Economic Implications of Learning by Doing*, 29 *REV. ECON. STUD.* 155 (1962).

²⁵ *BOSTON CONSULTING GROUP, PERSPECTIVES ON EXPERIENCE* (Boston Consulting Group 1972).

²⁶ See Theodore Paul Wright, *Factors Affecting the Cost of Airplanes*, 3 *J. AERONAUTICAL SCI.* 122 (1936) or, more recently, C. Lanier Benkard, *Learning and Forgetting: The Dynamics of Aircraft Production*, 90 *AM. ECON. REV.* 1034 (2000). The literature on the learning curve is voluminous. Recent noticeable contributions include (but are not limited to) Paul S. Adler & Kim B. Clark, *Behind the Learning Curve: A Sketch of the Learning Process*, 37 *MGMT. SCI.* 267 (1991); Willard I. Zangwill & Paul B. Kantor, *Towards a Theory of Continuous Improvements and the Learning curve*, 44 *MGMT. SCI.* 910 (1998); Eelke Wiersma, *Conditions that Shape the Learning Curve: Factors that Increase the Ability and Opportunity to Learn*, 53 *MGMT. SCI.* 1903 (2007).

is not firm-specific or worker-specific but can actually be shared. This feature motivates our policy proposal (explained in Part IV).

This proposal consists of mandating the exchange of query logs across search engines, which amounts to setting up an interorganizational information system and is related to the literature on electronic data interchanges. Prominent works have focused on the case where a single buyer tries to organize information exchanges with several suppliers. In our case, the exchange would be *reciprocal* between all search engines. Of importance is the finding that competitive effects from sharing information typically preclude universal voluntary adoption by rival firms.²⁷ Search logs have long been recognized as a rich source of information that can be used to improve search efficiency (among other things).²⁸

The search engine industry, although new, has already given rise to a number of academic studies.²⁹ David Evans and James Ratliff and Daniel Rubinfeld have looked at the larger online advertising industry.³⁰ Most technical papers have looked at some of the newest aspects of the sector (compared with standard yellow pages), in particular the disclosure of sponsored links alongside so-called organic results,³¹ the keyword auctions introduced to price them,³² or the substitutability between search engine advertising and the more traditional types of advertising.³³

²⁷ Frederick J. Riggins, Charles H. Kriebel & Tridas Mukhopadhyay, *The Growth of Interorganizational Systems in the Presence of Network Externalities*, 40 MGMT. SCI. 984 (1994); Eric T. G. Wang & Abraham Seidmann, *Electronic Data Interchange: Competitive Externalities and Strategic Implementation Policies*, 41 MGMT. SCI. 401 (1995).

²⁸ For accessible introductions, see Bernard J. Jansen, *Search Log Analysis: What It Is, What's Been Done, How to Do It*, 28 LIB. & INFO. SCI. RES. 407 (2006); Fabrizio Silvestri, *Mining Query Logs: Turning Search Usage Data into Knowledge*, 4 FOUND. & TRENDS IN INFO. RETRIEVAL 1 (2010).

²⁹ See Hal R. Varian, *The Economics of Internet Search*, 96 RIVISTA DI POLITICA ECONOMICA 9 (2006); Daniel F. Spulber, *The Map of Commerce: Internet Search, Competition, and the Circular Flow of Information*, 5 J. COMPETITION L. & ECON. 633 (2009).

³⁰ David S. Evans, *The Economics of the Online Advertising Industry*, 7 REV. NETWORK ECON. 359 (2008); James D. Ratliff & Daniel L. Rubinfeld, *Online Advertising: Defining Relevant Markets*, 6 J. COMPETITION L. & ECON. 653 (2010).

³¹ See Anindya Ghose & Sha Yang, *An Empirical Analysis of Search Engine Advertising: Sponsored Search in Electronic Markets*, 55 MGMT. SCI. 1605 (2009); Greg Taylor, *Search Quality and Revenue Cannibalization by Competing Search Engines* (Mimeo, Oxford Univ., 2010); Song Yao & Carl F. Mela, *A Dynamic Model of Sponsored Search Advertising*, 30 MARKETING SCI. 447 (2011).

³² See Yongmin Chen & Chuan He, *Paid Placement: Advertising and Search on the Internet* (Networks, Electronic Commerce, & Telecommunications (NET) Institute, Working Paper No.06-02, 2006); Benjamin Edelman, Michael Ostrovsky & Michael Schwarz, *Internet Advertising and the Generalized Second-price Auction: Selling Billions of Dollars Worth of Keywords*, 97 AM. ECON. REV. 242 (2007); Varian, *supra* note 29; Susan Athey & Glenn Ellison, *Position Auctions with Consumer Search*, Q. J. ECON. (forthcoming).

³³ Avi Goldfarb & Catherine Tucker, *Search Engine Advertising: Channel Substitution When Pricing Ads to Context*, 57 MGMT. SCI. 458 (2011); Avi Goldfarb & Catherine Tucker,

Neil Gandal and Rahul Telang, Uday Rajan, and Tridas Mukhopadhyay attempted early on to predict the general dynamics of the industry, which was then still in its infancy.³⁴ Those articles do not focus on, or identify, network effects. Neither does Rufus Pollock, who argues that the search engine industry will continue to evolve down its path toward monopoly, with deleterious consequences to welfare.³⁵ Pollock also calls for regulatory oversight, in particular the vertical separation of the “software” and “service” divisions of search engine firms.³⁶ Such an intervention, affecting the organizational or capital structure of the industry, has wide implications, and we believe that our more modest proposal is easier to implement.

III. THE MODEL

A. From Stylized Facts to Modeling

Search engines do not charge end users for running queries. Nevertheless, some are highly profitable.³⁷ Most of their revenues come from selling (targeted) advertisements related to search queries and displayed as “commercial results” or “sponsored links” next to the so-called organic links, which are the results of a search query generated by the search engine’s algorithm.

Over time, successful search engines have developed particular ways to select and price advertisements. The celebrated Google keyword auction (AdWords) is a prime example. Clearly, search engines are in the business of matching potential buyers (searchers) with sellers (advertisers). Thus, the theory of intermediaries, or *two-sided markets* in economics jargon, may be of relevance.³⁸ We do not want to downplay this important feature of the industry. However, it seems to us that the fact that the price on users’ side is

Substitution between Online and Offline Advertising Markets, 7 J. COMPETITION L. & ECON. 37 (2011).

³⁴ Neil Gandal, *The Dynamics of Competition in the Internet Search Engine Market*, 19 INT’L J. INDUS. ORG. 1103 (2001); Rahul Telang, Uday Rajan & Tridas Mukhopadhyay, *Market Structure For Internet Search Engines*, 21 J. MGMT. INFO. SYS. 137 (2004).

³⁵ Rufus Pollock, *Is Google the Next Microsoft? Competition, Welfare and Regulation in Online Search*, 9 REV. NETWORK ECON. 1 (2010).

³⁶ *Id.*

³⁷ Not all search engines are profitable. As of March 2010, “reports indicate that Redmond [Microsoft] has spent as much as \$5bn on its nine-month-old search revamp, and the company continues to pour cash into the would-be Google killer.” Cade Metz, *One Day, Bing Will Actually Make Money*, THE REGISTER, Mar. 2, 2010, http://www.theregister.co.uk/2010/03/02/ballmer_o_n_bing/. Compare this with the performance of search engines 2 and 3 in our model displayed in Figure 2.

³⁸ Varian, *The Economics of Internet Search*, *supra* note 29, and Evans, *supra* note 30, insist on that point. See Jean-Charles Rochet & Jean Tirole, *Two-Sided Markets: A Progress Report*, 37 RAND J. ECON. 645 (2006) for a technical overview of the theory. Jean-Charles Rochet & Jean Tirole, *Introduction to the Symposium on Two-sided Markets*, 3 COMPETITION POL’Y INT’L 146 (2007) introduce several less-technical papers.

always set to zero has become a strong norm in the industry. In addition, in the literature, it is a controversial question as to whether sponsored links bring direct positive utility to consumers.³⁹ As a result, the two-sidedness of the market may not be pronounced.⁴⁰ We thus follow an agnostic approach and assume that consumers derive neither positive nor negative utility from sponsored links.⁴¹ As we are not primarily interested in the advertising side, we assume that the advertising revenue of a search engine is proportional to its market share, which is broadly in line with the industry's figures. That is, advertisers are willing to pay a given price for "eyeballs" to search engines. This does not detract from the fact that every better targeted advertising is an important margin of innovation and competition in the industry. It is simply not the focus of attention in this article.

The search engine market is characterized by two additional important features: some degree of horizontal product differentiation and incomplete information of consumers about search engine quality with respect to a specific keyword. In a recent report, users were asked how they perceive the major search engines to be different.⁴² Google, for instance, is perceived to have a very simple design that completely focuses on their search box. In contrast, Bing's "feature-filled" image and video search is recognized. Moreover, "as opposed to Google," Yahoo!'s "auto-recommendation bar [...] offers smart recommendations." In addition, Bernard Jansen, Mimi Zhang, and Ying Zhang have shown that the relevance of results, as rated by users, is influenced by the name of the search engine, thus pointing to the importance of branding.⁴³

The perception of search engine differentiation leads to the fact that, before running a specific keyword, picture, or video search, consumers do not exactly know which search engine delivers the highest search quality for the item in which they are interested. This uncertainty partly stems from an asymmetric and unknown distribution of previous queries across search engines. Hence, before running a specific search, it is impossible to say whether this or that search engine delivers the highest quality results. Consumers can only rationally expect search engine quality to be different on average. Therefore, an appropriate model of the search engine market

³⁹ Chen & He, *supra* note 32; Athey & Ellison, *supra* note 32; Edelman, Ostrovsky & Schwarz, *supra* note 32; Taylor, *supra* note 31. Avi Goldfarb & Catherine Tucker, *Online Display Advertising: Targeting and Obtrusiveness*, 30 *MARKETING SCI.* 389 (2011) show that targeted advertising leads to negative externalities only when obtrusive.

⁴⁰ The French Competition Authority's online advertising sector inquiry reached the same conclusion. Avis No. 10-A-29 du 14 Décembre 2010 sur le Fonctionnement Concurrentiel de la Publicité en Ligne [Opinion No. 10-A-29 of 14 Dec. 2010 on the Competitive Operation of Online Advertising], Autorité de la Concurrence [Competition Authority] (Fr.).

⁴¹ Positive indirect network externalities on the users' side would only reinforce market tipping.

⁴² See uTest, *supra* note 18.

⁴³ See Jansen, Zhang & Zhang, *supra* note 16.

must deliver “smooth” outcomes, where a firm’s market share is monotonically increasing in its perceived average search quality, but where even a search engine with low perceived average quality retains a positive market share.

B. A Contest Model

As shown in the Introduction, today’s search engine market features one dominant firm that competes with two notable competitors.⁴⁴ Therefore, we start by modeling a triopoly market with firms 1, 2, and 3.

On the demand side, in our model, there is a unit mass of consumers, each of which has demand for one query. As has been the business practice since the birth of the industry, nominal prices for using a search engine are zero. We assume that the market is fully covered—that is, that quality is high enough for every consumer to use a search engine.

It is natural to appeal to a class of models that allow consumers to choose which search engine they want to use, on the basis of those engines’ characteristics, in particular their perceived quality level, as well as consumers’ own preferences. Discrete choice models of product differentiation allow consumers’ utility to be randomly shocked in a way that makes sure that all engines capture at least a fraction of demand.⁴⁵ In such models, consumers do not know in advance which product they will consume, and it is possible to compute clear measures of economic welfare, such as expected consumer surplus. To simplify the presentation, we take a shortcut and work with a model that fits the stylized facts outlined above (as well as the properties of the functional form for market shares that would be derived from standard discrete choice models). We model competition as a contest among search engines with simultaneous bids x_i , where x_i is firm i ’s search quality; $i \in \{1, 2, 3\}$. That is, search engines simultaneously and independently choose their quality level. The market share of firm i is then given by $D_i = x_i / \sum_{j=1}^n x_j$, where $j \in \{1, \dots, n\}$, and $n = 3$ firms are active in the market. Production of quality x_i comes at a cost, $C(x_i) = x_i / N_i$, where N_i is the “installed base” of firm i , that is, the amount of previous search queries run on i . Without loss of generality, we assume $N_1 \geq N_2 \geq N_3 \equiv 1$. Moreover, each firm bears a fixed cost F for its operations.

This formulation interprets x_i as the quality of search engine i perceived by consumers. The cost to create a certain level of perceived quality depends on the resources spent on improving the search engine’s algorithm and on

⁴⁴ Since 2010, Yahoo! has used Bing’s search technology and does not invest in its own search technology anymore; see *supra* note 3. In the analysis below, we discuss the incentives of search engines 2 and 3 to exit the market and merge.

⁴⁵ For an exposition of those models, see SIMON P. ANDERSON, ANDRE DE PALMA & JACQUES-FRANCOIS THISSE, *DISCRETE CHOICE THEORY OF PRODUCT DIFFERENTIATION* (MIT Press 1992).

the amount of private data accessible, which makes it cheaper to produce any quality level. It is as if search engines learn to produce quality more cheaply by using their stock of past queries.

Following these assumptions, search engine i solves the following program:

$$\max_{x_i} \pi_i = \frac{x_i}{x_1 + x_2 + x_3} p - \frac{x_i}{N_i} - F, \quad (1)$$

where p is the exogenously given advertising revenue associated with one consumer.⁴⁶

C. Analysis of the Triopoly Case

It is possible to characterize the behavior of each search engine and solve for the equilibrium. For details, we point to Part A in the Appendix, where we display the relevant computations. Figure 1 displays equilibrium quality levels and market shares as a function of N_1 , the amount of private data to be searched by firm 1.

Interestingly, although we model a simple one-shot game, N_i can be interpreted in a dynamic way: the market share of firm i in some period t influences the relative amount of private data to which firm i has access in period $t + 1$. Consequently, if firm 1 has access to more data than firms 2 and 3 at one point of time, the equilibrium predicts that, *ceteris paribus*, this advantage increases over time.⁴⁷

This result implies that the market is *tipping*, that is, firm 1 is producing ever higher perceived quality—and gains ever higher market share—whereas firms 2 and 3 decrease their respective quality levels—and market shares—over time. However, the survival of the weakest search engine, firm 3, is called into question as soon as the data access advantage of firm 1 or 2, expressed by N_1 and N_2 , respectively, is sufficiently large. It is indeed costly to produce quality so that advertising revenues, and thus market share must be high enough to maintain positive profits. Therefore, the model predicts

⁴⁶ In a first approximation, the marginal cost of running an additional query can be taken to be zero. In any case, variable costs can always be subsumed into the p variable, which would then stand for net revenue per user. This formulation implicitly assumes that quality affects the fixed cost of production rather than the variable cost. This is likely: variable costs mostly come from the huge energy requirements needed to run server farms, whereas quality is directly related to the work of engineers and software developers.

⁴⁷ We are aware of the fact that a static model is not the best tool to study market dynamics. The dynamic extension of our model can be worked out, especially if there is no quality persistence over time. We use the static model to illustrate our main ideas. The search engine industry arguably meets the conditions identified by Joshua S. Gans, *When Is Static Analysis a Sufficient Proxy for Dynamic Considerations? Reconsidering Antitrust and Innovation*, in 11 INNOVATION POLICY AND THE ECONOMY 55 (Josh Lerner & Scott Stern eds., Univ. of Chicago Press 2010) for static analysis to be a sufficient proxy for dynamic considerations in innovative industries.

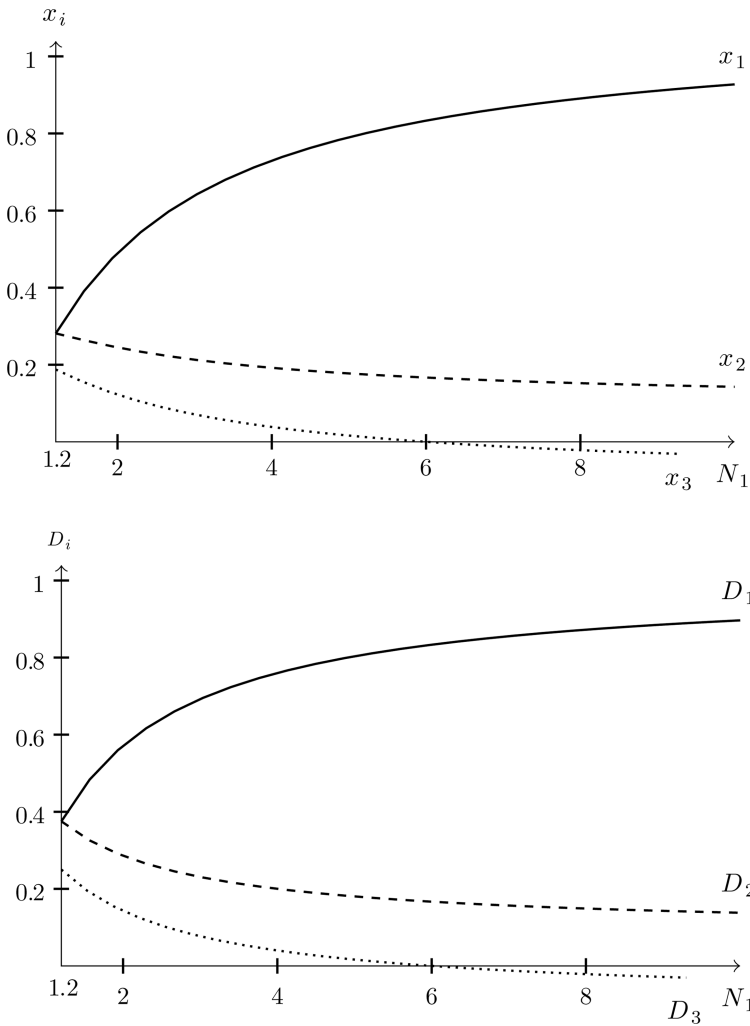


Figure 1. Numerical example for $p = 1$, $N_2 = 1.2$. Top: equilibrium quality, bottom: market shares.

that firm 3 sooner or later exits the market, and the market structure turns from a triopoly into a duopoly.

Before turning to the duopoly case, however, let us analyze the welfare effects of network externalities in the triopoly model. Equilibrium profits (π_i) are easily calculated by substituting equilibrium quality levels into equation (1). Producer surplus (PS) is the sum of all firms' profits. Expected consumer surplus (CS) is found by averaging equilibrium quality levels weighted with the market shares of active firms. Summing up producer surplus and consumer surplus, we get total surplus (W). Figure 2 displays a graphical representation of firms' profits and total welfare as a function of N_1 .

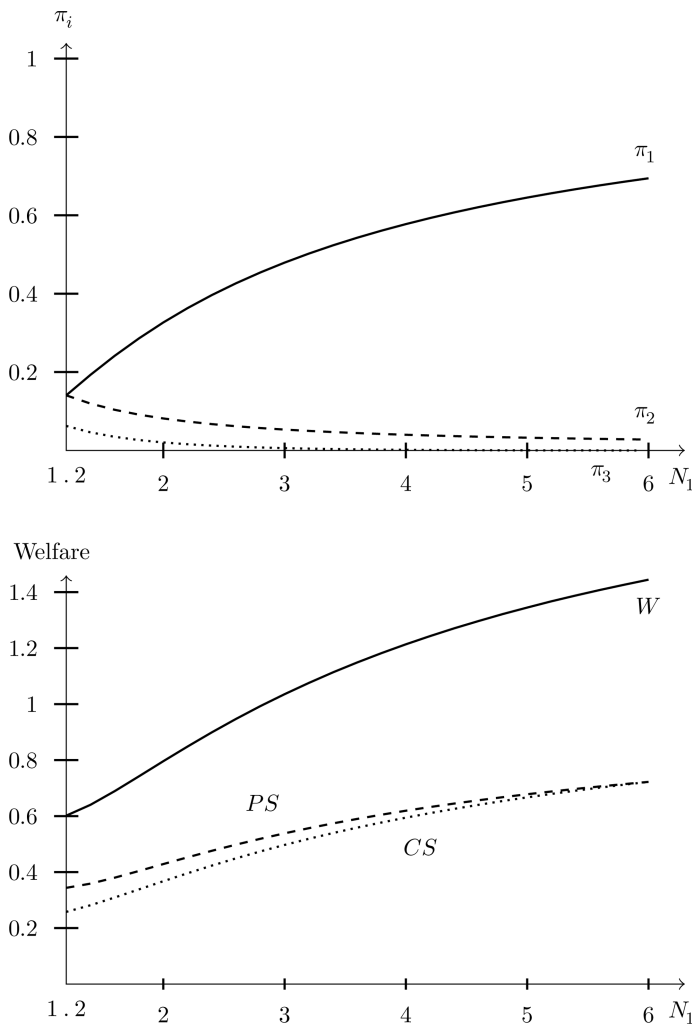


Figure 2. Numerical example for $p = 1$, $F = 0$, $N_2 = 1.2$, $N_1 \in [1.2, 6]$. Top: equilibrium profits, bottom: welfare.

Figure 2 shows that firm 1’s profit increases in N_1 , which implies that, by virtue of the argumentation outlined above, its profit also increases over time. Instead, firm 2’s and firm 3’s profits decrease over time. Hence, in our model, it is very profitable to be the market leader and to maximize the advantage over competitors in accessing (private) data about past queries.

Notably, consumer surplus and welfare are also increasing in N_1 (and in N_2). This effect stems from the fact that network externalities decrease the cost of producing quality: more and more consumers enjoy the increasing quality of the market leader.

D. The Duopoly Case

If firm 3 exits the market, each of the remaining firms 1 and 2 solves the following simplified program, (1):

$$\max_{x_i} \pi_i = \frac{x_i}{x_1 + x_2} p - \frac{x_i}{N_i} - F. \quad (2)$$

For simplicity and without loss of generality, we set $N_2 \equiv 1$. It is again straightforward to solve for a unique equilibrium in quality levels with positive market shares. The results (explained further in Part B in the Appendix) show that the duopoly market is developing in the same way as the triopoly market: the market tips toward a single search engine. In line with the ever-decreasing market share of firm 2, for every $F > 0$, the profit of firm 2 turns negative if N_1 is sufficiently high. It follows that our model predicts that a duopoly, too, is not a stable market structure in the long run if the market leader retains its advantage regarding access to private data. In effect, the industry has the character of a natural monopoly. Therefore, we are led to study equilibrium and welfare effects in the monopoly case.

E. The Monopoly Case

There are two variants of the monopoly model with potential applicability to the search engine industry. Part C of the Appendix provides computations of both. The benchmark result is the case of a *pure* or *uncontested monopoly*. We show that a monopolist that does not fear any competition sets the quality to a minimum (acceptable) level. Still, consumers would use this search engine, in the absence of alternatives, which would drive up the monopolist's profit. Unsurprisingly, this situation would be dismal for consumer surplus, total welfare, and the monopolist's incentive to invest in quality—that is, to innovate.

Importantly, our results imply that the extent of network externalities virtually does not play any role as long as the market is monopolized and no potential entrant is in sight. The monopolist has no incentive to produce positive quality and, therefore, its cost advantage created by access to private data is not exploited in equilibrium.

The second—and more realistic—variant of the monopoly model is the case of a *contestable monopoly*. Here the monopolist faces a potential (re-) entrant but may be able to prevent entry by making use of an appropriate “limit strategy.” To study this case, we consider the following sequential game, which we solve in Part C in the Appendix. First, the incumbent, firm 1, sets quality x_1 . Second, the potential entrant, firm 2, decides whether to enter the market for a cost $K \geq 0$. Third, if firm 2 enters the market, it sets quality x_2 . Finally, demands are realized, as before.

Given this structure, firm 1 can predict how firm 2 would behave—what quality it would produce—if it entered the market at the second stage.

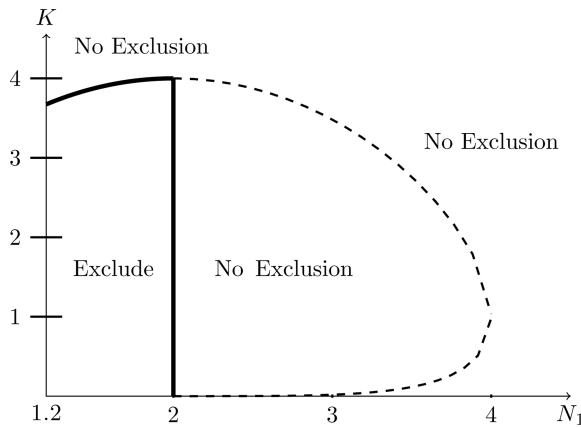


Figure 3. Numerical example of (non) exclusion incentives in a contestable monopoly, for $p = 1$, $F = 0$.

Therefore, firm 1 can calculate what entry would mean for its own profits and decide whether it wants to deter or accommodate it. The key tradeoff that arises for firm 1 is whether it wants to set a rather high quality, which we denote by x_1^{lim} in the Appendix, and enjoy monopoly, or set a rather low quality, $x_1^{Stackelberg}$, which saves on cost but does not necessarily foreclose the market.

In our parametric example, we find that, if the advantage in private data access of firm 1 is sufficiently large (that is, if $N_1 \geq 2$), then firm 2 cannot enter the market *and* gain a positive market share, even if firm 1 sets $x_1^{Stackelberg}$. Hence, in this case, it is not even necessary for firm 1 to foreclose the market by making use of a limit-quality strategy.⁴⁸

In contrast, if firm 1’s advantage in private data access is modest (such that $N_1 < 2$), we find that firm 2’s cost of market entry, K , becomes crucial. If K is rather low, firm 1 sets x_1^{lim} . In this case, the entrant knows that it would also need to set a rather high quality to compete with the incumbent. This high quality would be so costly for firm 2, however, that it could not operate profitably. It follows that firm 2 abstains from entering the market if the incumbent sets the limit quality, x_1^{lim} . Finally, if K is high, firm 1’s best choice is to set $x_1^{Stackelberg}$. This implies that firm 2 could indeed enter the market and gain a positive market share. However, it could not recoup the market entry cost with the modest operational profits this would bring. Understanding this, firm 2 would not enter the market in this case either.

Figure 3 maps all applicable constraints. Firm 1 plays $x_1^{Stackelberg}$ unless both N_1 and K are low, in which case it actively forecloses the market by

⁴⁸ Even in this case, firm 1 cannot set quality as low as in the absence of competition (that is, $x_1 = \varepsilon$) because then firm 2 could set a higher quality and (almost) capture the entire market demand, thereby making a profit.

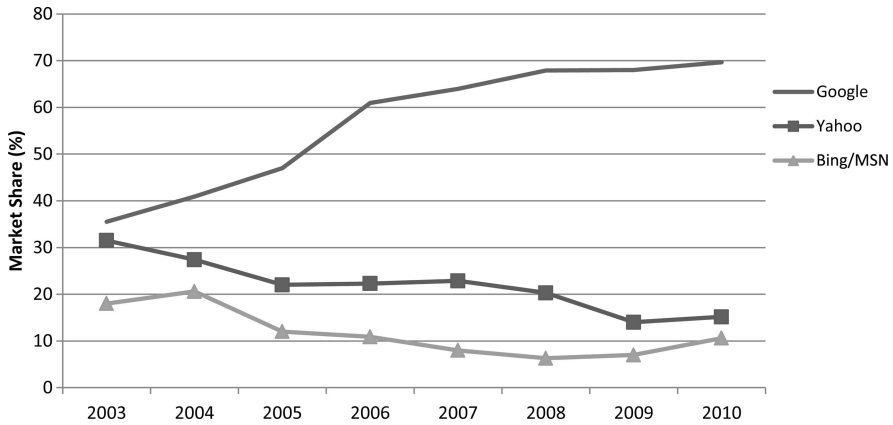


Figure 4. U.S. market shares in search referrals to other websites. Sources: WebSide Story; Nielson Hitwise.

setting the limit quality, x_1^{lim} . The outcome of all parameter combinations is the same, though: A monopoly is a stable market structure.

F. Reality Check

The model generates several testable implications. First, it predicts market tipping (as shown in the top panel of Figure 1): the market share of the dominant firm is expected to increase more and more, whereas the market shares of the other firms are expected to decrease. Second, the model predicts substantial profit growth for the market leader and decreasing profits for the following firms (as shown in the bottom panel of Figure 2). Third, as a consequence of the second point, the model predicts market exit of one follower.

These predictions are well reflected in the history of the search engine market since 2003, when Google became the market leader. Figure 4 shows the actual development of market shares of the top three search engines in the United States. In this figure, Google takes the role of firm 1, whereas Yahoo! and Bing take on firms 2 and 3, respectively.

Although starting from roughly the same market share as Yahoo! in 2003, Google managed to increase its U.S. market share up to nearly 70 percent by the end of 2010.⁴⁹ In line with that success, Yahoo!'s and Microsoft's search engines (first MSN, then Bing) halved their market shares—from a combined 50 percent in 2003 to 25 percent in 2010. The model's second

⁴⁹ The development of market shares on a global level followed a similar pattern in the last decade. The main difference was that Google's dominance was even more pronounced on a global scale, reaching about 85 percent market share at the end of 2010.

prediction also corresponds to the empirically observed development of profits: Google's profit rose by 36 percent to 2.51 billion dollars in the second quarter of 2011,⁵⁰ whereas Bing has appeared to lose money.⁵¹ Finally, the model's third prediction is reflected by the de facto market exit of Yahoo!, which sold its search and advertising business to Microsoft in early 2010. We conclude that, although our model is simple and stylized, it can reproduce several key developments that are well in line with the latest historical developments in the search engine industry.

IV. POLICY PROPOSAL

We have shown that, absent any other major changes, network externalities in the search engine market can be expected to drive out competitors of the dominant firm and to lead to a stable monopoly. Due to the adverse welfare effects that this development would have (as we explain in detail below), we state our policy proposal:

All search engines should be required to share their (anonymized) data on clicking behavior of users following previous search queries among each other and among new entrants.

In the following discussion, we first analyze the economic case on which this proposal is based. Second, we discuss the technical and practical feasibility of the proposal. Finally, we sketch the potential legal basis, provided by regulation and competition law, that could justify the proposed market intervention.

A. The Competitive Oligopoly Case

Consider the triopoly market studied above and assume, for now, that our policy proposal could be implemented without frictions. We call this the competitive oligopoly case.⁵² Technically, our proposal implies that all search engines get access to all context-specific data available in the industry, N , where:

$$N \equiv N_1 + N_2 + N_3. \quad (3)$$

We solve this model for equilibrium quality levels and the resulting welfare measures in Part D of the Appendix.

Now we are in a position to compare the effect of our policy proposal on key variables with the respective effect of the market structures analyzed before. Figure 5 depicts the comparisons of consumer surplus and total welfare as a function of the installed base of the most successful search

⁵⁰ See After Record Profits: Google Stock Shoots Up, FinancesJournal.com, <http://financesjournal.com/taxes/record-profits-google-stock-shoots-7114.html>.

⁵¹ See Metz, *supra* note 37.

⁵² The results are qualitatively identical whether we consider two, three, or more firms.

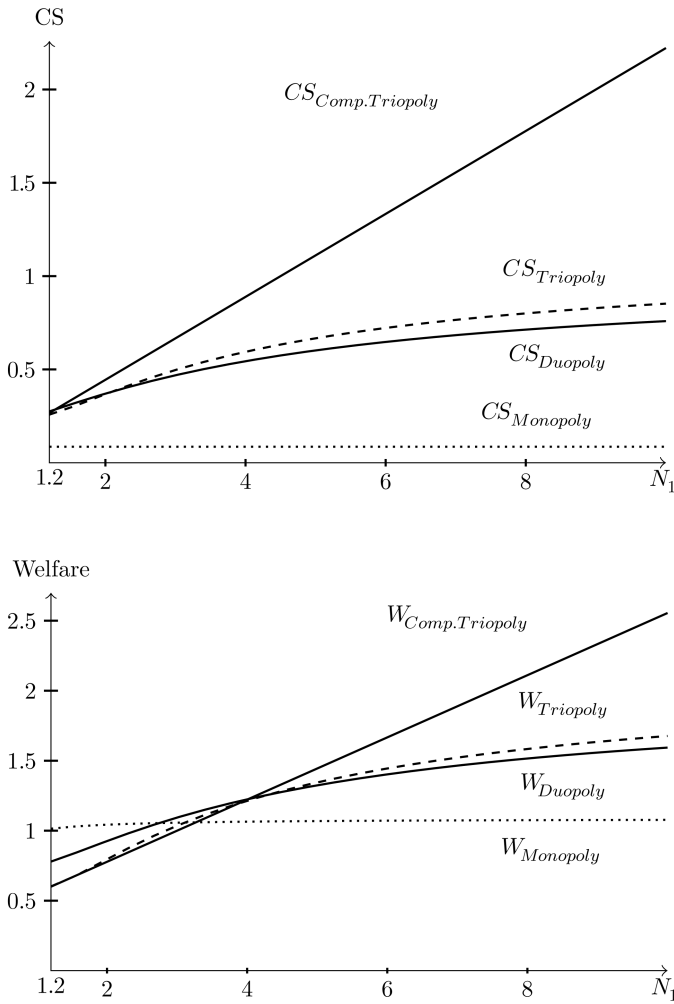


Figure 5. Numerical example for $p = 1$, $F = 0$, $N_2 = 1.2$, $K = 0.5$. Top: consumer surplus, bottom: welfare across market structures.

engine, N_1 . There, “monopoly” is based on the equilibrium values generated by the limit-quality case.⁵³

Figure 5 shows that consumer surplus increases in the level of competition (from monopoly to competitive triopoly) and in the extent of network externalities (apart from the limit-quality monopoly case), depicted on the horizontal axis. It also shows that consumer surplus and welfare in market structures without intervention are of the same scale as the one of the

⁵³ As our analysis has shown, quality and welfare under an uncontested monopoly are even lower.

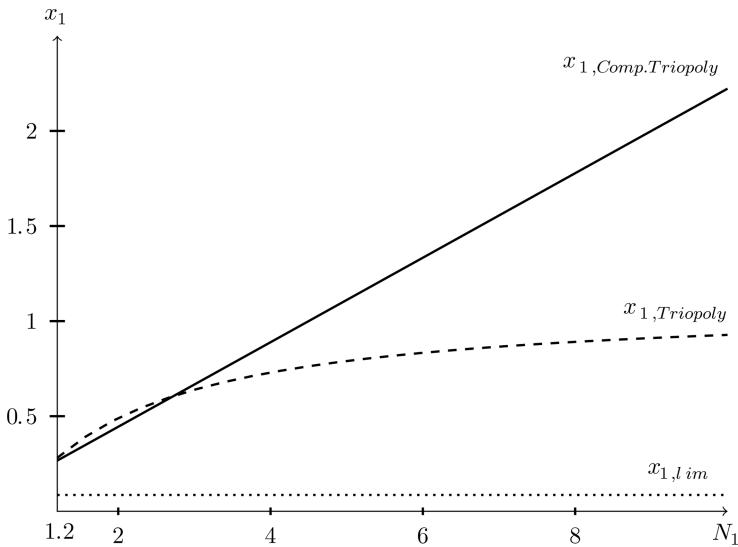


Figure 6. Numerical example of the quality of firm 1 under different market structures, for $p = 1, F = 0, N_2 = 1.2, K = 0.5$.

intervention case, as long as N_1 is sufficiently small. With growing N_1 , however, the competitive triopoly case becomes more and more attractive and, for high N_1 , clearly dominates the other cases. The key tradeoff under a competitive triopoly is that, on the downside, it multiplies the fixed cost of producing quality because several firms are active in the market and spend on high quality production. On the upside, the competitive triopoly makes sure that all consumers get high search quality, not only the consumers of the dominant firm.

Importantly, the reason for the superiority of the competitive oligopoly over alternative market structures is rooted in the high quality levels that intense competition produces. Figure 6 depicts the equilibrium quality of firm 1 under several market structures.

The comparison of the current triopoly with the competitive triopoly is interesting. In both cases, quality increases in N_1 —or over time, using our earlier interpretation. In the current triopoly, however, the dominant firm reduces its “rate of innovation” (proxied by the slope of its quality curve) when the market tips more and more in its favor. This effect does not exist under the competitive triopoly. There, no search engine can rest on its merits because the only way to sustain its market share and profits is to invest all efficiency gains that come from the exploitation of network externalities in better quality. As a result, producer surplus is unaffected by N , whereas consumer surplus monotonically increases in N .⁵⁴

⁵⁴ See equations (A.29) and (A.30) in the Appendix.

On the other hand, given that even under the competitive triopoly all three firms make positive profits (provided the fixed cost of operation is not prohibitive), it would be false to claim that equal access of all search engines to the complete pool of previous search data wipes out incentives to do business in this market or to enter it in the first place.

In this Part, we have not taken into account the cost of our policy proposal yet, which was assumed to be implementable “without frictions” above. We will discuss potential frictions below. Nevertheless, at this stage, it is important to note that our main theoretical result, the dominance of the competitive oligopoly over the alternative market structures analyzed, from a consumer surplus and total welfare perspective, qualitatively holds, even if our policy proposal came at substantial transaction costs. In our model, such costs could be reflected by higher F . In the long run, however—that is, if N grows sufficiently large, which is inevitable as long as search engines operate and consistently collect data on user behavior—consumer surplus and total welfare increase to levels that are unrivaled by alternative market structures.⁵⁵ The reason is that intense competition between search engines based alone on the merits of the search algorithm provides better incentives to the firms to produce high-quality products than the rent enjoyed by a dominant firm that exploits a competitive advantage created by network externalities.

B. Technical Feasibility and Practical Implementation of our Policy Proposal

Above, we analyzed the economic effects of our proposal. But even if the positive economic effects are pronounced in theory, how realistic is our proposal?

Surprisingly, support for the technical feasibility of granting other parties access to large amounts of private data has come from an unexpected entity: Google. On October 13, 2010, Facebook, the world’s largest online social network, with more than 500 million users, and Bing, Microsoft’s search engine, announced an alliance. At the heart of it lies the idea that Bing delivers search results on the basis of the recommendations of the searcher’s Facebook friends, in addition to impersonal search recommendations. One day later, on October 14, Google’s then-CEO Eric Schmidt commented on the deal with the quote placed at the start of this article: “There’s always a concern that large private collections of data are not available to search engines. . . . We’ve taken a position, both in a religious and in a business

⁵⁵ All or a fraction of the old query data may stop being relevant after some time. Thus, it is possible that exponential decay or truncation impacts the evolution of N over time. That would not change the qualitative predictions of the model: a firm that has been dominant in the recent past would presently benefit from a competitive advantage.

perspective, that the world is better off if you take the information that you're assembling and make it accessible."⁵⁶

This position "is in line with the welfare superiority of the competitive oligopoly case analyzed above. Moreover, the statement indicates that it is technically feasible to "take the information that you're assembling and make it accessible" even if the "private collection of data" is "large."

Furthermore, it is straightforward to understand both the Bing-Facebook alliance and Google's reaction to it by drawing on our analysis: Bing has just increased N_2 (or decreased the distance $|N_1 - N_2|$). Google replied that they want to increase N_1 (or to increase the distance $|N_1 - N_2|$). The motivation for both actions is clear if one inspects how the equilibrium profits of firms 1 and 2 under the current triopoly depend on N_1 and N_2 .⁵⁷

Next, apart from technical feasibility, how could our policy proposal be implemented effectively? Without going into too much detail, we perceive two avenues for implementation. First, if the number of major competing search engines is limited, as is the case today, it might work that data on previous searches are directly and bilaterally exchanged between search engines, under a monitoring regime. This would allow for a relatively timely delivery of the data as no technical or administrative detours would need to be taken. What would be essentially needed is a body achieving standardization of the way search engine query logs are reported (and anonymized) along with a compliance regime.⁵⁸

The second major way the data exchange could be organized is to create a new hub, to which all search engines would need to deliver their private data. In exchange, they would get access to all other data saved in the hub. This method is potentially costly, as a new structure (and perhaps several of them for technical or legal reasons) would need to be set up and permanently operated, although all search engines may not have the means to collect and mine all data.

Identifying which of these two ways is technically efficient would need to be determined by information and computer scientists, who understand the hardware, software, and network problems involved better than we do. In both cases, though, the enforcement and monitoring of the policy proposal would need to be given to a public agency—or several agencies, which could be located in several jurisdictions.⁵⁹ We leave the details of these issues, which combine computer science and public choice theory, for future research.

⁵⁶ See Boyd, *supra* note 1.

⁵⁷ See equations (A.10) and (A.11) in the Appendix or Figure 2.

⁵⁸ Eytan Adar, *User 4XXXXX9: Anonymizing Query Logs* (presented at the World Wide Web Conference, 2007), available at <http://www.cond.org/anonlogs.pdf>. and Syam Menon & Sumit Sarkar, *Minimizing Information Loss and Preserving Privacy*, 53 MGMT. SCI. 101 (2007) explore ways to anonymize large data sets such as query logs.

⁵⁹ We are aware of the potential public choice difficulty that handing over enforcement and monitoring to a public agency could create. This is why we suggest to have at least two technical and institutional infrastructures do this job, which should be ideally placed in at

Note that, in absolute terms, our proposal implies that all search engines, including the market leader, gain extra information on users' clicking behavior. Hence, if, say, the picture search of one search engine is better than its search for travel-related information, but another search engine has a comparative advantage in travel-related search, both search engines would obtain higher perceived quality in their weaker search domain after our proposal was implemented. In relative terms, of course, the market leader loses the advantage created by having access to more query log data—which is the very purpose of our proposal.

C. Sketching the Legal Issues

The possibility for public intervention in the market for search engines must be studied from a legal point of view. Here, we make only a very modest start and sketch the major legal issues: the applicability of competition law and the protection of privacy.

The first issue of interest is whether competition law can be used to implement our proposal. Suppose that rivals of dominant search engines asked one another to share their data regarding previous queries (possibly against payment). They might receive a negative reply that could be construed as a refusal to deal. Could such a refusal constitute a monopolization practice unlawful under Section 2 of the Sherman Act, for instance?

Case law provides for a set of limiting conditions under which a unilateral refusal to supply an essential input can be viewed as anticompetitive and call for antitrust relief.⁶⁰ On the basis of U.S. Supreme Court cases *Otter Tail* and *Aspen*, U.S. lower courts have recognized a duty for a firm with monopoly power to deal with its rivals under certain conditions.⁶¹ Those include (beyond the fact that the monopolist indeed denied use of the essential facility to a rival) (1) the fact that the property to which access is sought is indispensable to the production process, (2) the fact that the facility cannot be easily duplicated, and (3) the fact that sharing the facility is feasible. There is quite some uncertainty about this line of case law, which has always been criticized by scholars and which the U.S. Supreme court has always made a point of never endorsing as such.⁶²

least two jurisdictions. Competition between (or at least duplication of) agencies may preempt any attempt to abuse any one agency's power.

⁶⁰ Here, we follow EINER ELHAUGE & DAMIEN GERADIN, *GLOBAL COMPETITION LAW AND ECONOMICS* (Hart Publishing 2007).

⁶¹ See *Otter Tail Power Co. v. U.S.*, 410 U.S. 366 (1973); *Aspen Skiing Co. v. Aspen Highlands Skiing Corp.*, 472 U.S. 585 (1985).

⁶² See, most recently, *Verizon Commc'ns v. Law Offices of Curtis V. Trinko*, 540 U.S.398 (2004).

EU case law, although different, provides for similar conditions. Those were laid out in the famous *Commercial Solvents*, *Oscar Bronner*, and *IMS* cases and their limitations apparently were confirmed in the *Microsoft* case.⁶³ They include (1) the indispensability of the property to which access is sought, (2) the fact that the refusal to grant access is susceptible to excluding effective competition on the downstream market, and (3) the fact that the refusal has no objective, legitimate justification. An additional condition, in the case of intellectual property, derived from *IMS*, seems to be that rivals use it to introduce a new product to the market, but this requirement seems rather formalistic following *Microsoft*.

We take the criteria in turn to determine whether the essential facilities doctrine can be used to implement our proposal.

First, on essentiality, it is hard to argue that access to context-dependent data generated by previous queries is *absolutely* indispensable. It makes it easier for engines to return relevant answers by giving them data scale (and immediacy), but it certainly does not preclude them from investing heavily into improvements in the sophistication of the search algorithm or in the collection of other kinds of data.⁶⁴ At the same time, in *Aspen* and *Kodak*, the U.S. Supreme Court recognized a duty to deal even in the absence of true essentiality.⁶⁵

Second, duplication in U.S. case law plays the same role as the effective competition test in EU law. Both criteria aim at capturing the ability of competitors to exert meaningful competitive pressure on the owner of the essential input in case access is denied. In the context of search engines, duplication is clearly impossible. It is not a matter of money: a search engine can generate voluminous query logs only if end users massively choose to use it to place search queries now, which may well be impossible if the data needed to return relevant results are simply not there.

Third, the U.S. criterion of feasibility has been interpreted as meaning more than technical feasibility to include economic feasibility. That is, a duty to deal was denied whenever there seemed to be an objective

⁶³ See *Commercial Solvents: Cases 6 and 7/73*, *Commercial Solvents and Others v. Comm'n*, 1974 E.C.R. 223; *Case 7/97, Oscar Bronner GmbH & Co KG v. Mediaprint Zeitung und Zeitschriftenverlag GmbH & Co.*, 1998 E.C.R. I-7791; *Case C-148/01, IMS Health GmbH & Co.OHG v. Health GmbH & Co.KG*, 2004 E.C.R. I-5039; *Case T-201/14, Microsoft Corp. v. Comm'n*, 2007 E.C.R. II-3601.

⁶⁴ However, see Grimes, Tang & Russell, *supra* note 16, who argue that, although engines can use field or laboratory experiments and instrument online panels to acquire data, query logs contain “irreplaceable information for understanding the scope of resources that a search engine needs to provide for the user.” *Id.* at 1.

⁶⁵ See *Aspen*, 472 U.S. 585; *Eastman Kodak v. Image Technical Services*, 504 U.S. 451 (1992). In *Aspen*, the case revolved around the possibility for one ski domain manager to issue bundled tickets giving access to all mountains in one ski resort, including some managed by another company. In *Kodak*, eighteen independent service providers were complaining that Kodak had restricted access to replacement parts needed to service Kodak equipment.

justification for the refusal, such as efficiency, customer satisfaction, cost reduction, quality, and so on, as the EU allows. Technical complications do not make data exchange impossible in our view, as discussed above. Exchange would also be nonrivalrous, in the sense that granting access to competitors would not undermine the ability of data set owners to use them to serve their customers. Thus, there seems to be little room to claim that *ex post* efficiency reasons objectively justify a refusal to deal. Of course, a defense could be mounted with regard to the deleterious effect that any duty to deal would have on *ex ante* investment incentives. That is true of any essential facility case. Notice, however, that the data advantage of a dominant firm on the market for search engines is a *by-product* of its past success: even if it had known that it would later be subjected to a duty to deal, it would not have refrained from returning as relevant results as possible to users' queries.

All in all, it appears possible to invoke the essential facility doctrine but one should expect a difficult discussion about the interpretation of the essentiality requirement. An additional drawback is that antitrust remedies can apply only to firms which have been found to be in a dominant position in the relevant market in the EU, or to have monopoly power for monopolization to be actionable under Section 2 of the Sherman Act in the United States. Hence, only dominant search engines could face an obligation to share information about previous queries under antitrust laws; those are therefore unfit to allow public authorities to run a *universal* data-sharing scheme.

This said, if at the end of its current investigation into Google's practices, the Commission were convinced that these practices did breach Article 102 TFEU, it could, independently of any discussion about essential facilities, choose to mandate our proposal as an appropriate remedy. Indeed, Regulation 1/2003 vests the Commission with the necessary powers to impose such a remedy to "prevent repetition of the infringement and . . . eliminate its consequences."⁶⁶ Such elimination could well take the form of taking proactive steps aiming at restoring competition on the market, as suggested by Frank P. Maier-Rigaud, Per Hellström, and Friedrich Wenzel Bulst.⁶⁷

Another legal basis for our proposal is for public authorities to rely on regulatory intervention. We are aware of the costs usually associated with such interventions. However, in this case, we believe that the limited nature of our proposal would help to keep those costs under control. Indeed, what would be needed is a body achieving standardization of the way search engine query logs are reported (and anonymized) and monitoring compliance. The

⁶⁶ This power was recognized by case law before the enactment of the regulation. See Case C-62/86 AKZO Chemie BV v. Commission, 1991 E.C.R. 3359, ¶155.

⁶⁷ Frank P. Maier-Rigaud, Per Hellström & Friedrich Wenzel Bulst, *Remedies in European Antitrust Law*, 76 ANTITRUST L.J. 43 (2009).

question as to how to price access to data is thornier. Successful search engines could indeed argue that the proposal amounts to regulatory takings of proprietary data sets. The issue of access pricing is notoriously involved,⁶⁸ but it is parts and parcel of regulatory practice. We note, in addition, that the alternative to intervention is not the perpetuation of the current situation but, bar any breakthrough innovation, straight monopolization of the industry. Therefore, the economic cost of nonintervention is given by the depressed incentives to innovate for the dominant search engine.

A second issue of legal interest concerns the respect of the right to privacy of search engine users. Let us mention upfront that, as alluded to in footnote 9, search engines routinely obtain (with consent) more private data about users than we advocate to share. If a search engine offers additional services, such as an e-mail program, other productivity tools or a web browser, and a user stays logged in to those services while using the search engine, it is possible to match data on clicking behavior with much more detailed information at the individual user level. Under our policy proposal, these data would not need to be shared, which implies that search engines could further exploit some competitive advantage generated by their use.

Whether query logs constituted “personal data” *per se* in the sense of the European Union’s Data Protection Directive⁶⁹ was debated for a while. It is now clear that the ability to trace back the physical address of users on the basis of their IP address (or, worse, to clearly identify them as persons on the basis of a unique identifier derived from a permanent cookie) implies that search engines’ logs contain “personal data.”⁷⁰ Moreover, the obligations derived from the Directive apply to all search engines doing business in the European Economic Area, independently of the location of their headquarters (or servers). Hence, all search engines potentially fall within the scope of the Directive. Retention periods put objective limits to the amount of data that can be exchanged under our proposal, but irreversible anonymization of logs is generally seen as one way search engines can comply with the Directive by eliminating the personal dimension of data.⁷¹

⁶⁸ For introductory surveys, see Mark Armstrong, *The Theory of Access Pricing and Interconnection*, in 1 HANDBOOK OF TELECOMMUNICATIONS ECONOMICS 295 (Martin E. Cave, Sumit K. Majumdar & Ingo Vogelsang eds., North-Holland 2002); Ingo Vogelsang, *Price Regulation of Access to Telecommunications Networks*, 41 J ECON. LIT. 830 (2003).

⁶⁹ Council Directive 95/46, 1995 O.J. (L 281) (EC).

⁷⁰ See Opinion 1/2008 on Data Protection Issues Related to Search Engines, Advisory Working Party (adopted Apr. 4, 2008) (EC), Data Protection *available at* http://ec.europa.eu/justice/policies/privacy/docs/wpdocs/2008/wp148_en.pdf. The Working Party was created by Council Directive 95/46, art. 29 (EC).

⁷¹ See the source mentioned in footnote 3 for this assessment. See Google Anonymizing Search Records To Protect Privacy, Search Engine Land, <http://searchengineland.com/google-anonymizing-search-records-to-protect-privacy-10736> for details on how anonymization can work in practice.

Indeed, to preempt any privacy concerns, our policy proposal refers to anonymized data on search sessions only.

V. CONCLUSION

Given our model, it is an open question as to how Google managed to become the market leader and to outcompete both Yahoo! and Microsoft by 2003. Likely explanations are that Google's search algorithm was in fact of drastically higher quality than its competitors' during that stage or that query data mining was not yet in its mature phase. Apparently, Yahoo! and other search engines active before Google's market expansion were not able to exploit the network externalities present in the industry decisively. Since Google has taken over the pole position, however, we do not know whether it has increased its lead in market shares because its algorithm quality has become even better than its competitors' in relative terms or whether its success has mainly happened due to network externalities, in the absence of drastic innovation. Our model suggests that the latter effect is sufficient to explain the market development throughout the last years.

We believe that, to reap the full benefits of competition in this highly innovative market, it is necessary to intervene and reinstall merit-based competition. Our results have shown that the rate of innovation, quality, consumer surplus, and total welfare are higher if search engines only compete with their actual algorithm qualities instead of under the current situation, where a dominant firm may still innovate but has less incentives to do so at the margin, given the tipping market effect.

This proposal is in line with the DOJ's (2010) decision, which stated that the Yahoo!-Microsoft alliance in February 2010

will enhance Microsoft's competitive performance because it will have access to a larger set of queries, which should accelerate the automated learning of Microsoft's search and paid search algorithms and enhance Microsoft's ability to serve more relevant search results and paid search listings, particularly with respect to rare or 'tail' queries. The increased queries received by the combined operation will further provide Microsoft with a much larger pool of data than it currently has or is likely to obtain without this transaction. This larger data pool may enable more effective testing and thus more rapid innovation of potential new search-related products, changes in the presentation of search results and paid search listings, other changes in the user interface, and changes in the search or paid search algorithms. This enhanced performance, if realized, should exert correspondingly greater competitive pressure in the marketplace.⁷²

We argue that the authorities should not stop at clearing the Microsoft-Yahoo! deal but should push for a level playing field in the search engine market more actively. Such intervention would present policymakers with the same dilemma as other interventions in high-tech sectors: one can

⁷² U.S. DOJ Statement on Microsoft & Yahoo! 2010, *supra* note 17.

well argue that technical innovation will come soon in the future in such a drastic manner that the current firms and technologies will become obsolete. In that case, it is preferable simply to let the current market leader reap the profits from its past research effort and hope that incentives for breakthrough innovation remain sufficient in the meantime. That is, however, a bet, and one may well want to tilt the market toward higher levels of incremental innovation now by restoring firms' ability to compete neck-and-neck. Whatever the final decision, an implicit stance is taken on the kind and level of innovative activity that is desirable in the search engine market.⁷³

APPENDIX

I. COMPUTATIONS

A. The Triopoly Case

The model is a static game with complete information. Solving equation (1) for all three firms gives the following system of reaction functions:

$$x_1 = \sqrt{pN_1(x_2 + x_3)} - x_2 - x_3, \quad (A.1)$$

$$x_2 = \sqrt{pN_2(x_1 + x_3)} - x_1 - x_3, \quad (A.2)$$

$$x_3 = \sqrt{p(x_1 + x_2)} - x_1 - x_2. \quad (A.3)$$

Solving this system for optimal quality levels gives the following unique Nash equilibrium with positive market shares:

$$x_1^* = \sqrt{\frac{p^2 N_1^2 N_2^2}{(N_2 + N_1(1 + N_2))^2}} - \frac{4pN_1 N_2^2}{(N_2 + N_1(1 + N_2))^2}, \quad (A.4)$$

$$x_2^* = \frac{2pN_1 N_2 (N_1(N_2 - 1) + N_2)}{(N_2 + N_1(1 + N_2))^2}, \quad (A.5)$$

$$x_3^* = \frac{2pN_1 N_2 (-N_1(N_2 - 1) + N_2)}{(N_2 + N_1(1 + N_2))^2}. \quad (A.6)$$

⁷³ For a reading of the European *Microsoft* case along similar lines, see Pierre Larouche, *The European Microsoft Case at the Crossroads of Competition Policy and Innovation: Comment on Ahlborn and Evans*, 75 ANTITRUST L.J. 933 (2009).

Nash equilibrium quality levels lead to the following market shares:

$$D_1 = 1 - \frac{2N_2}{N_2 + N_1(1 + N_2)}, \quad (A.7)$$

$$D_2 = 1 - \frac{2N_1}{N_2 + N_1(1 + N_2)}, \quad (A.8)$$

$$D_3 = \frac{N_1(1 - N_2) + N_2}{N_2 + N_1(1 + N_2)}. \quad (A.9)$$

Figure 1 displays equilibrium quality levels and market shares as a function of N_1 . We proceed by analyzing the welfare effects of network externalities in the triopoly model. Equilibrium profits are easily calculated by substituting equilibrium quality levels into equation (1). We obtain:

$$\pi_1 = \frac{(N_2 - N_1(1 + N_2))^2}{(N_2 + N_1(1 + N_2))^2} p - F, \quad (A.10)$$

$$\pi_2 = \frac{(N_2 + N_1(N_2 - 1))^2}{(N_2 + N_1(1 + N_2))^2} p - F, \quad (A.11)$$

$$\pi_3 = \frac{(N_2 + N_1(1 - N_2))^2}{(N_2 + N_1(1 + N_2))^2} p - F. \quad (A.12)$$

Producer surplus is the sum of all firms' profits:

$$\begin{aligned} \text{PS} &= \pi_1 + \pi_2 + \pi_3 \\ &= \frac{(3N_2^2 - 2N_1N_2(1 + N_2) + N_1^2(3 + N_2(3N_2 - 2)))}{(N_2 + N_1(1 + N_2))^2} p - 3F. \end{aligned} \quad (A.13)$$

We proxy consumer surplus by the equilibrium quality levels weighted with the market shares of the active firms:

$$\begin{aligned} \text{CS} &= D_1x_1^* + D_2x_2^* + D_3x_3^* = \\ &= \frac{2N_1N_2(3N_2^2 - 2N_1N_2(1 + N_2) + N_1^2(3 + N_2(3N_2 - 2)))}{(N_2 + N_1(1 + N_2))^3} p. \end{aligned} \quad (A.14)$$

Summing up producer surplus and consumer surplus, we get total welfare:

$$\begin{aligned} \mathcal{W} &= \frac{(N_2 + N_1(3N_2 + 1))(3N_2^2 - 2N_1N_2(1 + N_2) + N_1^2(3 + N_2(3N_2 - 2)))}{(N_2 + N_1(1 + N_2))^3} p \\ &\quad - 3F. \end{aligned} \quad (A.15)$$

Figure 2 displays a graphical representation of firms' profits and total welfare as a function of N_1 .

B. The Duopoly Case

It is straightforward to solve π_1 and π_2 equation (see equation (2)) for a unique Nash equilibrium in quality levels with positive market shares:

$$x_1^* = \frac{N_1^2}{(1 + N_1)^2}, \quad x_2^* = \frac{N_1}{(1 + N_1)^2}, \quad (A.16)$$

which leads to the following market shares:

$$D_1 = \frac{N_1}{1 + N_1}, \quad D_2^* = \frac{1}{1 + N_1}. \quad (A.17)$$

Equation (A.17) shows that the duopoly market is developing in the same way as the triopoly market: $\lim_{N_1 \rightarrow \infty} D_1 = 1$; $\lim_{N_1 \rightarrow \infty} D_2 = 0$. In words, the market is tipping.

Firms' profits, producer surplus, consumer surplus, and total welfare can be computed as in the triopoly model, which yields:

$$\pi_1 = \frac{N_1^2}{(1 + N_1)^2} - F; \quad \pi_2 = \frac{1}{(1 + N_1)^2} - F; \quad PS = \frac{N_1^2 + 1}{(1 + N_1)^2} - 2F, \quad (A.18)$$

$$CS = \frac{N_1 + N_1^3}{(1 + N_1)^3}; \quad W = \frac{1 + 2N_1 + N_1^2 + 2N_1^3}{(1 + N_1)^3} - 2F. \quad (A.19)$$

Given that the graphs of the duopoly case qualitatively resemble the graphs of the triopoly case without firm 3, we do not display them here.

C. The Monopoly Case

In the case of a pure (uncontested) monopoly, monopolistic firm 1 does not face any competition. Hence, it rationally sets quality $x_1^* = \varepsilon$, where ε is the smallest positive number that induces consumers to use its services. Nevertheless, it serves the entire market: $D_1 = 1$, which leads to profits of $\pi_1 = p - \varepsilon/N_1 \approx p$.

The welfare analysis of this case is equally straightforward. Consumers get a surplus of $CS = \varepsilon \approx 0$, whereas $PS = \pi_1$. Hence, total welfare sums to $W = p + (N_1 - 1)/N_1 \varepsilon \approx p$.

In the case of a contested monopoly, we solve the three-stage sequential game by backward induction, where we set $N_2 = 1$. At stage 3, given that firm 2 entered the market, it sets its quality, x_2 , according to its duopoly

reaction function:

$$x_2 = \sqrt{px_1} - x_1. \quad (A.20)$$

Note that this holds only for $p \geq x_1$. If $x_1 > p$, firm 2's best response is to set $x_2 = 0$.

At stage 2, firm 2 enters the market if, and only if, its expected profit from entry is positive. If we substitute equation (A.20) into firm 2's duopoly objective function, equation (2), assuming $N_2 = 1$, this requires:

$$\pi_2(x_1, F, K, p) = p - 2\sqrt{px_1} + x_1 - F - K > 0. \quad (A.21)$$

Solving equation (A.21) with the equality sign for zero shows that $\pi_2(x_1, F, K, p) \leq 0 \quad \forall x_1 \in I$, where the interval I is defined as $I : [K + F - 2\sqrt{(K + F)p} + p, K + F + 2\sqrt{(K + F)p} + p]$. The upper bound of this interval, however, is larger than p , which hurts the condition below (equation (A.20)). It follows that the only condition that firm 1 has to meet such that even firm 2's best response quality would leave it with a loss is $x_1 \geq K + F - 2\sqrt{(K + F)p} + p$. Given that firm 1 has no intrinsic value in providing a higher quality than necessary, it follows that, if it wants to keep firm 2 out of the market, firm 1 sets x_1 equal to the lower bound of I . In other words, firm 1's "limit quality" is:

$$x_1^{\text{lim}} = K + F - 2\sqrt{(K + F)p} + p. \quad (A.22)$$

At stage 1, when determining its quality level, firm 1 effectively also chooses its competition because its quality determines whether firm 2 enters the market or not. If it produces the limit quality, it keeps firm 2 out of the market.

If instead firm 1 sets x_1 such that firm 2 could possibly enter the market profitably, firm 2 will set its quality according to equation (A.20). Substituting this in firm 1's unconstrained duopoly profit function, equation (2), shows that firm 1 solves:

$$\max_{x_1} \quad \pi_1 = \sqrt{px_1} - \frac{x_1}{N_1} - F, \quad (A.23)$$

which is solved by firm 1's Stackelberg quality⁷⁴:

$$x_1^{\text{Stackelberg}} = \frac{N_1^2 p}{4}. \quad (A.24)$$

If firm 2 enters, it will react to $x_1^{\text{Stackelberg}}$ by setting x_2 according to equation

⁷⁴ We are aware that classical Stackelberg competition uses quantity levels, not quality levels, as a strategic variable. Still, we feel that our model is sufficiently close to the original Stackelberg model to warrant the use of its name.

(A.20), which gives:

$$x_2^{\text{Stackelberg}} = \frac{p}{4}(2N_1 - N_1^2). \tag{A.25}$$

Resulting market shares are:

$$D_1^{\text{Stackelberg}} = \frac{N_1}{2}; \quad D_2^{\text{Stackelberg}} = 1 - \frac{N_1}{2}, \tag{A.26}$$

which implies that firm 2 gives up and sets $x_2 = 0$ as soon as $N_1 \geq 2$. We obtain the following welfare results:

$$\begin{aligned} \pi_1^{\text{Stackelberg}} &= \frac{N_1 p}{4}; -F; & \pi_2^{\text{Stackelberg}} &= \frac{p}{4}(N_1 - 2)^2 - F - K; \\ \text{PS} &= \frac{p}{4}(4 + N_1(N_1 - 3))38 >; -2F - K; & \text{CS} &= \frac{pN_1}{4}(2 + N_1(N_1 - 2)); \cdot \\ & & W &38 >; = \frac{p}{4}(4 + N_1(N_1(N_1 - 1) - 1)) - 2F - K \end{aligned} \tag{A.27}] >$$

Firm 1 excludes firm 2 by setting x_1^{lim} if, and only if, $\pi_1^{\text{lim}} \geq \pi_1^{\text{Stackelberg}}$. This holds with the equality sign for $K = (1 + N_1 - \frac{N_1^2}{4})p \pm \sqrt{(4 - N_1)N_1 p^2 - F}$. Moreover, we have seen above that firm 2 can only get a positive market share if $N_1 \in [1,2]$. The combined effect of both constraints is depicted in Figure 3.

D. The Competitive Oligopoly Case

Each of the three firm maximizes its profits as given in equation (1) but with equal installed bases $N = N_1 + N_2 + N_3$. The resulting Nash equilibrium in quality levels is:

$$x_1^* = x_2^* = x_3^* = \frac{2}{9}Np \equiv x^{\text{comp}}, \tag{A.28}$$

which leads to market shares of one-third for each firm. The associated welfare results are:

$$\pi_1 = \pi_2 = \pi_3 = \frac{p}{9} - F; \quad \text{PS}^{\text{comp}} = \frac{p}{3} - 3F, \tag{A.29}$$

$$\text{CS}^{\text{comp}} = \frac{2}{9}Np; \quad W^{\text{comp}} = \frac{p}{9}(3 + 2N) - 3F. \tag{A.30}$$

Quality, consumer surplus, and total welfare are depicted in Figures 5 and 6.

